$5^{\text {th }}$ Junior Balkan Olympiad in Informatics

## heritage

Source code: heritage.c, heritage.cpp, heritage.pas Input file: heritage.in<br>Output file: heritage.out<br>Time limit: 0.3 s<br>Memory limit: 64 MB

The old Count D has a surface of land which he wants to leave as heritance to his n sons. The surface is delimited by an horizontal segment [AB] placed on the $0 x$ axis, two vertical segments [ $A P_{1}$ ] and $\left[B P_{m}\right.$ ], and a polygonal line $\mathrm{P}=\left[\mathrm{P}_{1} \mathrm{P}_{2} \ldots \mathrm{P}_{\mathrm{m}}\right]$ placed entirely upside the Ox axis. The Count D builds $\mathrm{n}-1$ vertical fences each of them connecting the [AB] segment with the polygonal line $P$. As a result $n$ parcels of land with different areas will be created and left as heritage to his sons. The Count D wishes that the following two conditions should be respected:

1. Each son should receive a parcel with an area directly proportional with his age.
2. The sum of the fences` lengths should be minimal.

## Task

Knowing the coordinates of the $m$ points $\mathrm{P}_{1}, \mathrm{P}_{2}, \ldots, \mathrm{P}_{\mathrm{m}}$ and his $\mathbf{n}$ sons` age, a parcelling, that respects the two conditions, must be determined.

## Description of Input

On the first line of the file heritage. in there are two natural numbers n and m with the meaning above. The following line contains $n$ natural numbers $v_{1}, v_{2}, \ldots, v_{n}$ representing the age of the $n$ sons. The following $m$ lines contain each a pair of natural numbers $x_{i}, y_{i}$, representing the coordinates of the points $P_{i}$. The numbers from each line are separated by one space.

## Description of output

The heritage. out file will have two lines. The first line will contain a real number representing the sum of the fences` lengths. The second will contain $\mathrm{n}-1$ real numbers.
The $k^{\text {th }}$ number ( $k=1,2, \ldots, n-1$ ) will represent the coordinate of the $k^{\text {th }}$ fence on the Ox axis.
The numbers from the second line will be given in the increasing order and will be separated by one space.

## Constrains and remarks:

- $1 \leq n \leq 8$
- $1 \leq m \leq 500$
- $1 \leq v_{i} \leq 50$
- $0 \leq \mathrm{x}_{1}<\mathrm{x}_{2}<\ldots<\mathrm{x}_{\mathrm{m}} \leq 32000$
- $1 \leq \mathrm{y}_{1}, \mathrm{y}_{2}, \ldots, \mathrm{y}_{\mathrm{m}} \leq 32000$
- The width of the fences are ignorable;
- 
- Each value will be assessed with a precision of 0.001 ;
- For the contestants that use $\mathrm{C} / \mathrm{C}++$, it is recommended the double type.
- Your program will obtain a $100 \%$ score if the output respects both conditions;
- Your program will obtain a $20 \%$ score if the output respects only the first condition.
$5^{\text {th }}$ Junior Balkan Olympiad in Informatics
Bistrița, 3-9 July 2011
Day 2


## Example

| heritage.in | heritage.out | Remarks |
| :---: | :---: | :---: |
| $\begin{aligned} & 24 \\ & 42 \\ & 21 \\ & 83 \\ & 101 \\ & 143 \end{aligned}$ | $\begin{aligned} & 1.000000 \\ & 10.00 \end{aligned}$ | It is built only $\mathrm{P}^{\text {one }}$ fence. <br> The fence is built at $x=10.00000$, the 4 years old son will receive the parcel from the left and the 2 years old son will receive the parcel from the right. This way both conditions are respected. <br> Analysis <br> If the fence is built at $x=6.54984$ the 2 years old son will receive the parcel from the left and the 4 years old son will receive the parcel from the right. This way only the first condition would be respected. <br> Any other position of the fence will not respect any of the two conditions. |

