

Day 2

## heritage

# **100 points**

Source code: heritage.c, heritage.cpp, heritage.pas Input file: heritage.in Output file: heritage.out Time limit: 0.3 s Memory limit: 64 MB

The old Count D has a surface of land which he wants to leave as heritance to his n sons. The surface is delimited by an horizontal segment [AB] placed on the Ox axis, two vertical segments  $[AP_1]$  and  $[BP_m]$ , and a polygonal line  $P=[P_1P_2...P_m]$  placed entirely upside the Ox axis. The Count D builds n-1 vertical fences each of them connecting the [AB] segment with the polygonal line P. As a result n parcels of land with different areas will be created and left as heritage to his sons. The Count D wishes that the following two conditions should be respected:

- 1. Each son should receive a parcel with an area directly proportional with his age.
- 2. The sum of the fences` lengths should be minimal.

### Task

Knowing the coordinates of the m points  $P_1, P_2, \ldots, P_m$  and his n sons` age, a parcelling, that respects the two conditions, must be determined.

### **Description of Input**

On the first line of the file heritage.in there are two natural numbers n and m with the meaning above. The following line contains n natural numbers  $v_1, v_2, \ldots, v_n$  representing the age of the n sons. The following m lines contain each a pair of natural numbers  $x_i, y_i$ , representing the coordinates of the points  $P_i$ . The numbers from each line are separated by one space.

### **Description of output**

The heritage.out file will have two lines. The first line will contain a real number representing the sum of the fences` lengths. The second will contain n-1 real numbers.

The k<sup>th</sup> number (k=1,2,...,n-1) will represent the coordinate of the k<sup>th</sup> fence on the Ox axis.

The numbers from the second line will be given in the increasing order and will be separated by one space.

### **Constrains and remarks:**

- 1 ≤ n ≤ 8
- $1 \le m \le 500$
- $1 \le V_i \le 50$
- $0 \le x_1 < x_2 < \ldots < x_m \le 32000$
- $1 \le y_1, y_2, \ldots, y_m \le 32000$
- The width of the fences are ignorable;
- •
- Each value will be assessed with a precision of 0.001;
- For the contestants that use C/C++ , it is recommended the double type.
- Your program will obtain a 100% score if the output respects both conditions;
- Your program will obtain a 20% score if the output respects only the first condition.



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Example		
heritage.in	heritage.out	Remarks
2 4 4 2 2 1 8 3 10 1 14 3	1.000000 10.00	It is built only one fence. P <sub>1</sub> $P_3$ $P_4$ A The fence is built at x=10.00000, the 4 years old son will receive the parcel from the left and the 2 years old son will receive the parcel from the right. This way both conditions are respected.
		Analysis $P_2$ $P_4$ $P_1$ $P_2$ $P_4$ If the fence is built at x=6.54984 the 2 years old son will receive the parcel from the left and the 4 years old son will receive the parcel from the right. This way only the first condition would be respected. Any other position of the fence will not respect any of the two conditions.